

Watch. Practice. Understand. | Lesson 333

2022 Calculus BC Logistic Growth Model (Rogowski 9.4)

Watch the matching video: <https://www.youtube.com/watch?v=BBk8W4tp5i4>

Practice focus: Logistic growth

Original extra practice matched to the listed lesson topic.

Name: _____ Date: _____ Show your reasoning and check units.

01 For $P' = 0.2P(1 - P/1000)$, find equilibrium populations.

02 For that model, where is the positive growth rate largest?

03 Evaluate $P' = 0.2P(1 - P/1000)$ at $P = 200$.

04 For $P(t) = 1000/(1 + 9e^{-0.2t})$, find $P(0)$ and its long-run limit.

Worked answers | Lesson 333

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Practice focus: Logistic growth

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01 For $P' = 0.2P(1 - P/1000)$, find equilibrium populations.

Set $P' = 0$: $P = 0$ and $P = 1000$.

02 For that model, where is the positive growth rate largest?

The rate is a concave-down quadratic in P , with vertex at $P = 500$.

03 Evaluate $P' = 0.2P(1 - P/1000)$ at $P = 200$.

$P' = 0.2(200)(0.8) = 32$ population units per unit time.

04 For $P(t) = 1000/(1 + 9e^{(-0.2t)})$, find $P(0)$ and its long-run limit.

$P(0) = 1000/10 = 100$. As $t \rightarrow \infty$, denominator tends to 1, so limit is 1000.